

## A Robust Approach for the Evaluation of Airport Pavement Bearing Capacity

Dr. Ying-Haur Lee, Tamkang Univ.  
Mr. Yao-Bin Liu, National Central Univ.  
Dr. Jyh-Dong Lin, National Central Univ.  
Dr. Hsiang-Wei Ker, Chihlee Inst. of Tech.  
Taiwan



The University of Illinois at Urbana-Champaign  
June 29-July 2, 2009, Champaign, Illinois, USA



## Outline

- ◆ I. Introduction
- ◆ II. Review of ACN/PCN Methodology
- ◆ III. Goodness Study of Existing Backcalation Results
- ◆ IV. Application of NDT Test Data
- ◆ V. Development of A Robust Approach
- ◆ VI. A Case Study for Rigid Pavements
- ◆ VII. Concluding Remarks



2

## I. Introduction

- ACN/PCN Method Adopted by ICAO
  - for reporting airfield pavement bearing capacity
- Selecting Evaluation or Design Inputs
  - Should consider the mean and standard deviation, **but currently only the mean value was used** (AC 150/5370-11A)
  - "For a more conservative evaluation and design, the mean value minus one standard deviation (or the so-called 85% confidence level) may be used" (AC 150/5320-6D, AC 150/5370-11A)
- Research Approach → The concepts of random sampling, central limit theorem, and confidence intervals for hypothesis testing were adopted to derive a more consistent and repeatable PCN value



3

## II. Review of ACN/PCN Methodology



4

## ACN Determination

- Expressing the relative structural effect of an aircraft on a specified pavement type and a standard subgrade category
- By equating the thickness derived for a specified airplane landing gear to the thickness derived for a single wheel load (DSWL) at a standard tire pressure of 181 psi (1.25 MPa)
- Flexible Pavement
  - Boussinesq elastic layer solution
  - Four levels of subgrade strength (CBR)
  - 10,000 coverages
- Rigid Pavement
  - Westergaard interior loading solution on Winkler foundation
  - Four levels of subgrade strength (k)
  - Concrete working stress = 399 psi (2.75 MPa)
- ACN = 2 \* DSWL (in 1000 kg)



## Subgrade Strength Category

Subgrade Category Code	Flexible Pavement	Rigid Pavement	
	Subgrade CBR	Subgrade k-value (MN/m <sup>3</sup> )	Subgrade k-value (pci)
A (High)	15 (CBR ≥ 13)	150 (k ≥ 120)	552.6 (k ≥ 442)
B (Medium)	10 (8 < CBR < 13)	80 (60 < k < 120)	294.7 (221 < k < 442)
C (Low)	6 (4 < CBR ≤ 8)	40 (25 < k ≤ 60)	147.4 (92 < k ≤ 221)
D (Ultra Low)	3 (CBR ≤ 4)	20 (K ≤ 25)	73.7 (k ≤ 92)



## PCN Determination

- Expressing the relative load-carrying capacity of a pavement in terms of a standard single wheel load

60 / R / B / W / T	PCN Value	Pavement Type	Subgrade Category	Allowable Tire Pressure	Method Used
A Numerical Value	R (Rigid) F (Flexible)	A (High) B (Medium) C (Low) D (Ultra Low)	W (No limit) X (≤ 1.5 MPa) Y (≤ 1.0 MPa) Z (≤ 0.5 MPa)	T (Technical) U (Using Aircraft)	

- A particular PCN value can support an aircraft that has an ACN value equal to or less than the pavement's PCN value for unrestricted operations without weight restrictions



## COMFAA Software

Flexible Computation Function	Rc (psi)	Metric
A	3.0	46.75
B	3.0	46.75
C	3.0	46.75
D	3.0	46.75



## Factors Affecting PCN Assignment

- PCN method used
- Use of empirical or mechanistic based methods
- Evaluation method used
- Pavement structural life
- Method to derive an annual traffic volume
- Method to backcalculate material properties
- Different transfer functions, etc.

Note: PCN values can vary over 200% using different theories and evaluation technologies (Stet 2005)

Origin Method	PCN	Code
Flexible Pavement		
- CBR method S-77-1	55	FBWT
- PCASE-CBR	78	FBWT
- PCASE-LEA	69	FBWT
- Shell 85%	86	FBWT
- Barker et al	56	FBWT
- U.S. Corps of Engineers	64	FBWT
- APDS-MWHGL-data	43	FBWT
Rigid Pavement		
- PCA-PDLB	77	RCWT
- PCASE-Westerzaard	75	RCWT
- PCASE-LEA	79	RCWT
- UEC (Ref. 36)	78	RCWT
- Domanchini (Ref. 38)	66	RCWT
- Corps of Engineers	81	RCWT
- Vencon 1992	71	RCWT

Note: Flexible ACN of B747-400 at MTOW/OEW is 64.22; Rigid ACN of B747-400 at MTOW/OEW is 7

## III. Goodness Study of Existing PCC Backcalation Results

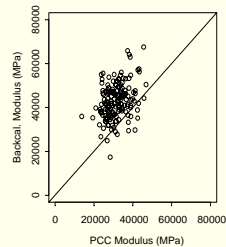
(Using LTPP DataPave Release 18.0)



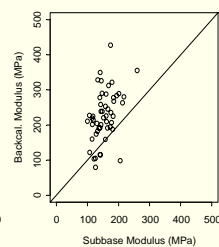
10

## Comparison of Lab Tested vs. Backcalc. Layer Moduli (1/2)

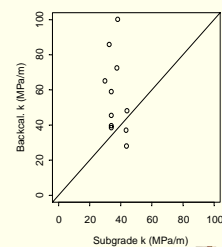
(a) PCC surface layer



(b) subbase layer



(c) subgrade



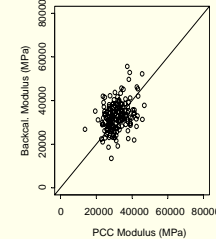
Winkler Foundation (Average ratios about 1.4, 1.5, 1.5)



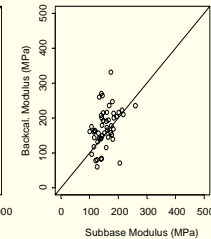
11

## Comparison of Lab Tested vs. Backcalc. Layer Moduli (2/2)

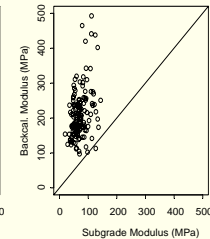
(d) PCC surface layer



(e) subbase layer



(f) subgrade



Elastic Solid Foundation (Average ratios about 1.0, 1.1, 3.0)



12

## Relationship of Elastic Modulus and Modulus of Subgrade Reaction (1/3)

- **FHWA-RD-00-086 Report (2001):**  
Backcalculation of layer parameters for LTPP Test Sections using GPS and SPS data

$$k = 0.296E_s$$

Statistics :  $R^2 = 0.872$ ,  $SEE = 9.37$ ,  $N = 596$



13

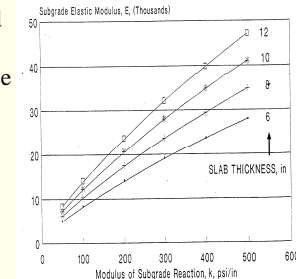
## Relationship of Elastic Modulus and Modulus of Subgrade Reaction (2/3)

- Barenberg (2000) indicated the theoretical difference using elastic solid and dense liquid foundations

$$w_e = \frac{Pl_e^2}{3\sqrt{3}D} = w_k = \frac{Pl_k^2}{8D}$$

$$\rightarrow 0.6495 * l_k^2 = l_e^2$$

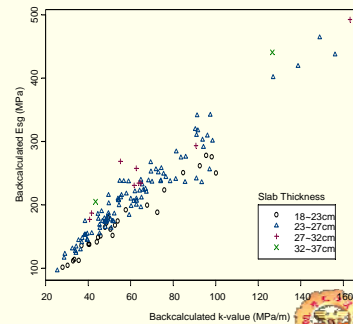
$$\rightarrow E_s^{4/3} = 283.7 * h * k$$



14

## Relationship of Elastic Modulus and Modulus of Subgrade Reaction (3/3)

- The aforementioned relationship was further verified by comparing the backcalculated  $E_s$  and  $k$  values from the LTPP database
- **Slab thickness did have significant effects on this relationship**



$$E_s = 0.9015(k * h)^{3/4}$$

Statistics :  $R^2 = 0.9524$ ,  $SEE = 15.87$ ,  $n = 138$



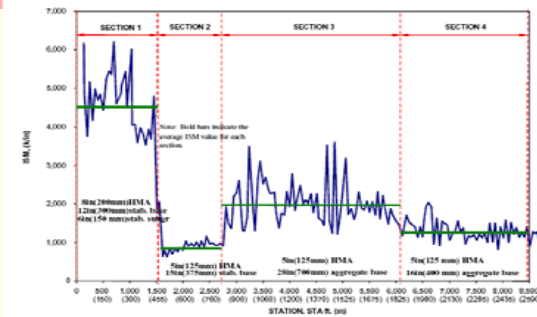
15

## IV. Treatment & Application of NDT Test Data



16

## Subdivide the Raw NDT Data Into Several Homogeneous Sub-Sections



Question: How many sub-sections?

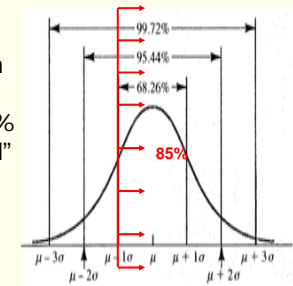


17

## Obtaining a Representative Evaluation or Design Input

(1/2)

- Based on the assumption of normal distribution, "the mean value minus one standard deviation (or the so-called 85% confidence level) may be used" (AC 150/5370-11A)



- $\Pr(-1 < Z < 0) + \Pr(0 < Z < \infty)$   
 $= 0.3413 + 0.5 \doteq 85\%$



18

## Obtaining a Representative Evaluation or Design Input

(2/2)

- What if the probability distribution function of the population is unknown and is not always normally distributed?

→ Chebyshev's Rule: the probability that any random variable differs from its mean by at least  $k$  standard deviations is less than or equal to  $1/k^2$ , in which  $k > 1$

$$P(|X - \mu| \geq k\sigma) \leq \frac{1}{k^2}$$

- The so-called 85% confidence level (or reliability) is only true when the population is normal



19

## V. Development of A Proposed Robust Approach

- Use the concepts of random sampling, central limit theorem, and confidence intervals for hypothesis testing
- This robust approach includes:
  - determine the number of sample units to be surveyed
  - determine a representative design input for the entire runway
  - obtain a single PCN value as usual



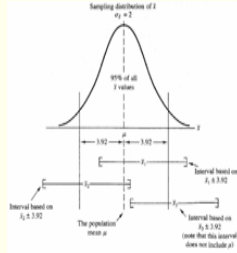
20

## Determine the Number of Sample Units to be Surveyed

$$\bar{X} - \mu = Z_{\alpha/2} \frac{S}{\sqrt{n}} \leq e$$

$$\bar{X} - \mu = t_{n-1, \alpha/2} \frac{S}{\sqrt{n}} \frac{\sqrt{N-n}}{\sqrt{N-1}} \leq e$$

$$\rightarrow n = \frac{NS^2}{(e^2/4)(N-1) + S^2}$$



Note: Already adopted by the ASTM (D5340-98) in pavement condition index (PCI) procedure (Shahin 1994)



21

## Determine a Representative Evaluation or Design Input

- A single representative design input for the entire runway pavement may be determined by the lower limit of 95% confidence level (1-tail)

$$\mu = \bar{X} - t_{n-1, \alpha} \frac{S}{\sqrt{n}}$$



22

## VI. A Case Study for Tech. Evaluation of Rigid Pavements



23

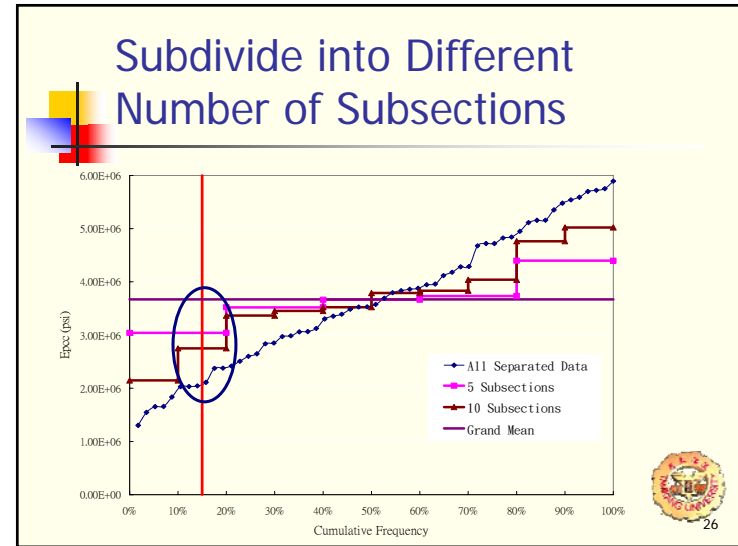
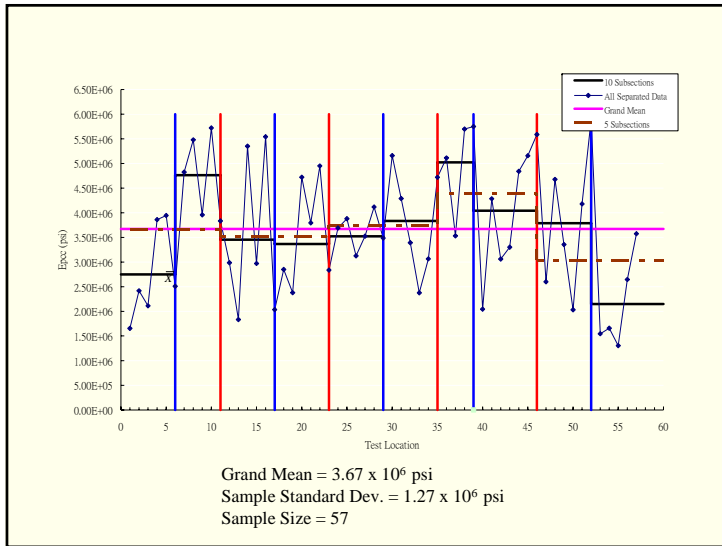
## Example Rigid Airfield Pavement Traffic Data

Airplane	Operating Weight, lbs	Tire Pressure (psi)	ACN (R/C)	** P/C	Annual Departures	Coverages
B727-200	185,000	148	55	2.92	400	2,740
B737-300	130,000	195	38	3.79	6,000	31,662
A319-100	145,000	173	42	3.18	1,200	7,547
B747-400	820,000	200	68	3.46	3,000	17,341
B767-300ER	370,000	190	58	3.60	2,000	11,111
DC8-63	330,000	194	62	3.35	800	4,776
A300-B4	370,000	205	67	3.49	1,500	8,595
B777-200	600,000	215	77	4.25	300	1,412

\*\* Rigid P/C determined at 95 percent of gross load on main gear (effective k = 200 pci, h = 14 in., MR = 700 psi, Ec = 4E+06 psi)



24



### Results of Using Different Evaluation Methods

Methods	Different Evaluation Methods	Representative Epc (psi)	Estimated Mr (psi)	Calculated Allowable Gross Weight (lbs)	PCN
I	Grand Mean	$3.67 \times 10^6$	648.1	700,000	55.0/R/C/W/T
II	Grand Mean - 1 Std.Dev.	$2.40 \times 10^6$	592.8	640,000	48.6/R/C/W/T
III	5 Subsections (85%)	$3.04 \times 10^6$	620.7	671,000	51.9/R/C/W/T
IV	10 Subsections (85%)	$2.75 \times 10^6$	608.1	656,000	50.3/R/C/W/T
V	All Separated Data (85%)	$2.05 \times 10^6$	585.1	632,000	47.8/R/C/W/T
VI	95% Confidence	$3.33 \times 10^6$	585.1	684,000	53.3/R/C/W/T

→ Methods I ~ V (PCN = 48/R/C to 55/R/C), Method VI (PCN = 53/R/C)

- ### VII. Concluding Remarks <sup>(1/2)</sup>
- According to AC 150/5370-11A's recommendation, the mean value minus one standard deviation (or the so-called 85% confidence level) may be used to obtain a more conservative evaluation or design input.
  - Nevertheless, it was found that this procedure is not based on sound statistical principles especially when the probability distribution function of the population is almost always unknown and is not necessarily normal.

## VII. Concluding Remarks (2/2)

- Consequently, the concepts of random sampling, central limit theorem, and confidence intervals for hypothesis testing were adopted.
- It was proposed that a single representative design input for the entire runway pavement be determined by the lower limit of 95% confidence level (1-tail) to derive a more consistent and repeatable PCN value.
- A case study was conducted to illustrate the potential problems of the existing ACN/PCN procedure and the benefits of the proposed revisions.



29

## Acknowledgements

- Sponsored by National Science Council, and Do & Find Engineering Consultant CO., LTD., Taiwan
- Ms. Chia-Huei Lin for her hard work in the goodness study of existing backcalculation results



30

THANKS FOR YOUR ATTENTION

Questions?

A large graphic with the text 'THANKS FOR YOUR ATTENTION' in a curved banner at the bottom and 'Questions?' in a large, stylized font in the center. A horizontal line is positioned above the text. A small circular logo is in the bottom right corner.

31