

## 由面層撓度值回算鋪面彈性模數的初步研究

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## OBJECTIVES

- Major Deficiencies of Traditional Backcalculation Procedures
  - a Uniqueness Problem
  - n Iterative but Time-consuming Calculation
  - t Subjective Selection of Initial Trial Values and Input Data Ranges
  - a Violation of the Specified Convergence Criteria
- Scope: A Two-Layer Elastic Pavement System

## RESEARCH APPROACH

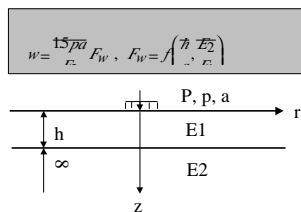
- Theoretical Investigation - Burmister (1943) and Scriver's (1973) Deflection Equations
- Identification of Functional Forms
- Validation of the Dominating Dimensionless Variables Identified
- Development of a Backcalculation Database
- Development of Backcalculation Prediction Equations
- Validation of the Proposed Prediction Equations

## CLASSIFICATION OF BACK-CALCULATION PROCEDURES

- Existing:
  - x Iterative Approach (BISDEF, ELSDEF, etc.)
  - t Data Base Approach (MODULUS)
- Proposed: (A New Approach)
  - r Integrate the Concept of Traditional Database Approach and Modern Regression Techniques
  - o Strive to Develop Prediction Equations to Allow "DIRECT" Modulus Calculations

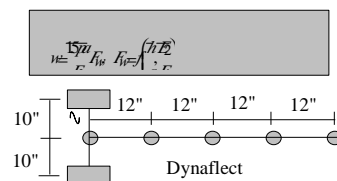
## DEVELOPMENT OF TWO-LAYER ELASTIC THEORY

- Burmister (1943)
  - ( A Uniformly Distributed Circular Load



## DEVELOPMENT OF TWO-LAYER ELASTIC THEORY (continue ...)

- Scriver (1973)
  - ( A Concentrated Load



## DYNAFLECT'S LOAD CONFIGURATION

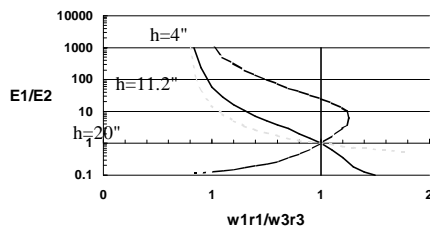
$$\frac{w_1 r_1}{w_3 r_3} = \frac{f_1 \left( \frac{E_2}{E_1}, \frac{r_1}{h} \right)}{f_3 \left( \frac{E_2}{E_1}, \frac{r_3}{h} \right)} = G \left( \frac{E_2}{E_1}, \frac{r_1}{h}, \frac{r_3}{h} \right)$$

- When  $r_1$ ,  $r_3$ , and  $h$  are known  $\implies$
- $w_1 r_1 / w_3 r_3$  is a function of  $E_2/E_1$

## LIMITATIONS OF BACK-CALCULATION PROGRAMS

- Assume there exists a Unique Modulus Combination
- Iterative but Time-consuming Calculations
- Results Affected by:
  - Different Initial Trial Values
  - Data Ranges
  - Specified Error Tolerance
  - Limited Number of Iterations

## Scrivner's Study (1973)



Dynaflect:  $a=1.41$ ",  $P=1000$  lbs,  $r_1=10$ ",  $r_3=26$ "

## UNIQUENESS PROBLEM FOR BACKCALCULATION

$w_1 r_1 / w_3 r_3$	$h > 11.2$ "	$h < 11.2$ "
1	Unique	None / Two
<1	Unique	None / Two

## DOMINATING MECHANISTIC VARIABLES (DIMENSIONLESS)

$$F N \frac{4 E_1}{3 P} w_1 r_1 N F \frac{E_2}{E_1} \frac{r_1}{h} \frac{h}{a}$$

$$w_1 r_1 N F \frac{E_2}{E_1} \frac{r_3}{h} \frac{h}{a}$$

- Identified through Theory for any NDT Devices
- Validated through Series of BISAR Runs

## Validation of Variable (h/a)

h/a	h in.	a in.	r1 in.	r3 in.	w1 mil	w3 mil	w1r1/w3r3
2.5	5	2	7.5	15	3.99	3.16	0.631
2.5	8	3.2	12	24	2.49	1.98	0.629
2.5	14	5.6	21	42	1.42	1.13	0.628

Note:  $r_1/h=1.5$ ,  $r_3/h=3$ ,  $E_2/E_1=100$ ,  
 $E_1=500,000$  psi,  $E_2=5,000$  psi,  $P=1,000$  lbs

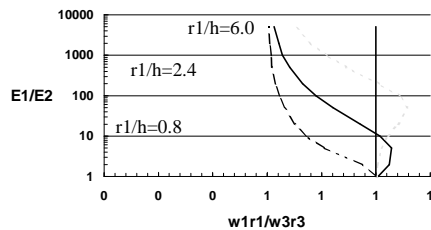
## A BACKCALCULATION DATABASE

- € Based on Four Dimensionless Variables Identified
- €  $E1/E2 = 1, 2, 5, 10, 20, 50, 100, 200, 500,$   
1000, 2000, 5000
- €  $r1/h = 0.8, 1.2, 1.8, 2.4, 3.6, 4.8, 6.0$
- €  $r3/h = 1.2, 1.8, 2.4, 3.6, 4.8, 6.0, 7.2$
- €  $h/a = 0.8, 1.3, 2.5, 3.5, 5.0$
- € ( $r1 > r3, P = 2400 \text{ lbs}, E2 = 1000 \text{ psi}, h = 10 \text{ in.}$ )
- € FORTRAN Programs Written for Batch Processing
- € Total of 1680 Data Sets

## USE OF THE DATABASE

- € Advantages:
  - "DIMENSIONLESS" Variables
  - Covers Almost All Data Ranges
  - Save Unnecessary Iterative Computation Time
- € A Computer Program, Look-up Tables or Figures for Linear Interpolation
- € "DIRECT" Calculation is Possible if "Uniqueness" is Guaranteed.

**$h/a=1.3, r1/r3=0.6$**



## PROJECTION PURSUIT REGRESSION

- € "Projection" (PPR) Algorithm by Friedman and Stuetzle, 1981
- € Capable of Modeling Variable Interactions
- € Model the Response Surface as a Sum of Nonparametric Prediction Functions of Explanatory Variables Using Local Smoothing Techniques

## "PROJECTION" (PPR) ALGORITHM

$$E_{\gamma} \nu_{\gamma}^2 = \text{Minimum}$$

Minimizing the Mean Squared Residuals:

$$E_{\gamma} \nu_{\gamma}^2 = \text{Minimum}$$

## TWO-STEP MODELING APPROACH

- € Use PPR Algorithm to Break down the Multi-Dimensional Response Surface into a Sum of Several Smooth Projected Curves, Which Are Graphically Representable in Two Dimensions
- € Use Traditional Linear and Nonlinear Regressions to Model Each Projected Curves Individually

**PROPOSED PREDICTION EQUATIONS FOR "DIRECT" CALCULATION - E1/E2**

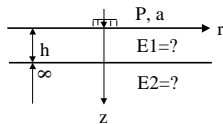
$$E[V^2] = \text{Minimum}$$

**PROPOSED PREDICTION EQUATIONS FOR "DIRECT" CALCULATION - E1**

$$E[V^2] = \text{Minimum}$$

**VALIDATION - A NUMERICAL EXAMPLE**

- A Two-Layer System  
h=10 in, P=3,000 lbs, a=7.69 in  
NDT Devices, r1=36 in, r3=60 in
- BISAR  
If E1=1.0 Mpsi, E2=5.0 Kpsi Known  
=> w1=0.00386 in, w3=0.0028 in
- Backcalculation  
(1) BISDEF Trials  
(2) Proposed Approach



**BISDEF TRIALS**

E1 Start Mpsi	E2 Start Kpsi	E1 Range Mpsi	E2 Range Kpsi	E1 Mpsi	E2 Kpsi	Within Tolerance*
0.5	3	0.1~2.5	1~50	1.61	4.71	Y, N
1.61 etc.	4.71 etc.	0.1~2.0	1~10	ERR	ERR	-
1.1	4.0	0.8~1.5	1~8	0.98	5.28	Y, N

\* - Absolute Sum of % Difference  
- Change in Modulus Values

**THE PROPOSED APPROACH**

- (1) Use for "Direct" Calculation  
Dimensionless Variables:  
h/a = 1.3, r1/h = 3.6  
r3/h = 6.0, w1r1/w3r3 = 0.827  
Use of the Prediction Models:  
=> log(E1/E2) = 2.28826, E1/E2 = 194.2  
=> log(Y) = 2.2475, Y = 176.8068  
=> E1 = 911,259 psi, E2 = 4,692 psi

**THE PROPOSED APPROACH**

- (2) Use as a Pre-Processor  
Assist in Selection of Initial Trial Values,  
Data Ranges to Speed Up the Convergence

E1 Start Mpsi	E2 Start Kpsi	E1 Range Mpsi	E2 Range Kpsi	E1 Mpsi	E2 Kpsi	Within Tolerance*
0.91	4.69	0.1~1.2	1~12	0.98	5.13	Y, Y

## CONCLUSIONS

- Discussed the "Uniqueness" Problem and Short Comings of Traditional Approach
- Proposed an Alternative Approach Using Database and Modern Regressions
- Identified Dominating Dimensionless Variables for More Complete Coverage
- Strive to Develop Prediction Equations to Allow "DIRECT" Modulus Calculations

## CONCLUSIONS (continue ...)

- Tentative Applications:
  - A Calculator, a Spreadsheet, or a Computer Program for "Direct" Modulus Calculations (Instantly)
  - A Pre-Processor of Traditional Backcalculation Programs In-field Modulus Determinations and NDT Data Checking
- Obtain More Accurate and Consistent Results

## LOOKING AHEAD ...

- Further Improve the Prediction Accuracy
- Investigate a Three- or Four-Layer System
- Must also Assure "Uniqueness" of Solutions
- Possible Use of Local Regression Techniques or Any Database Search Algorithms
- Lots of Research Remain to be Done!

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