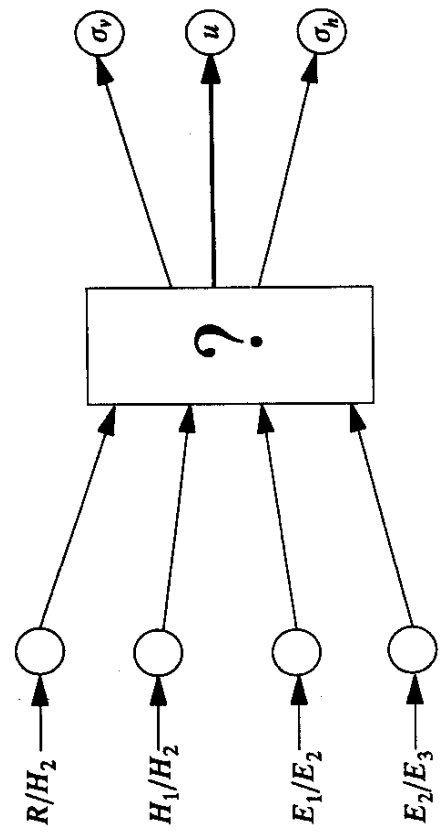
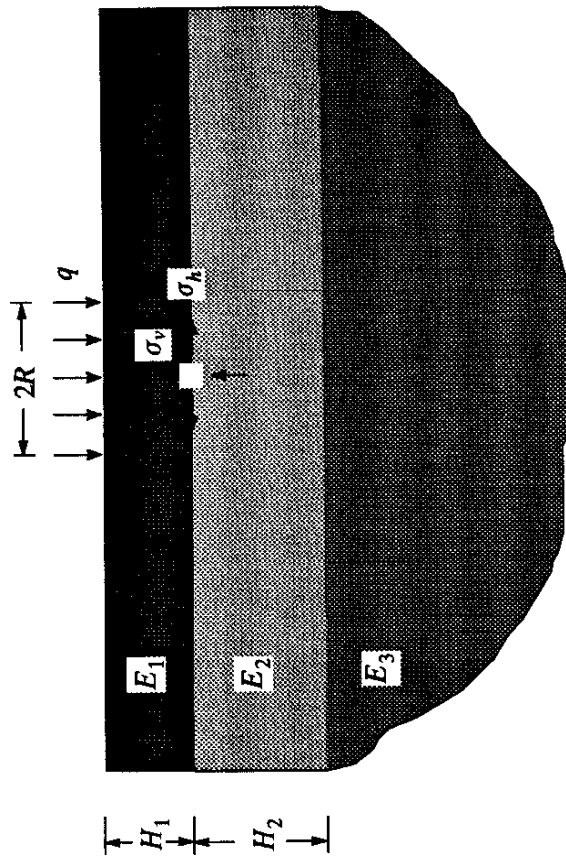


**THREE LAYER ELASTIC HALF SPACE**



**SUMMARY OF DATA**

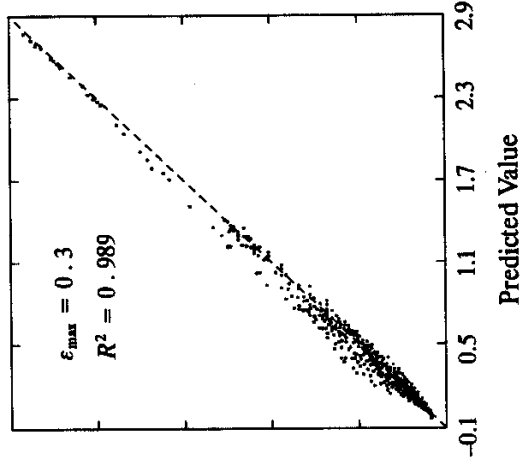
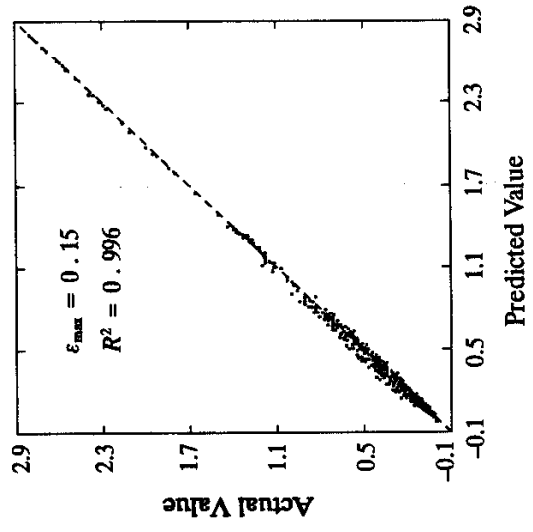
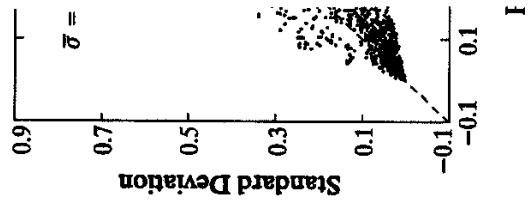
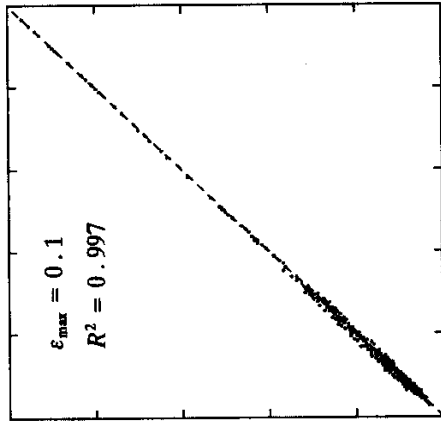
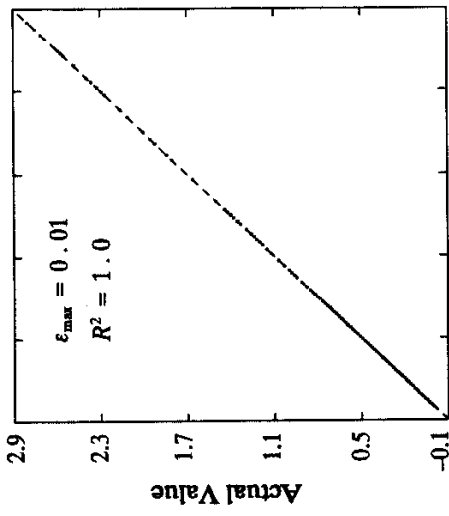
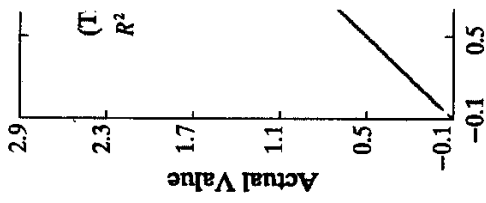
	DISPLACEMENT			HORIZONTAL STRESS			VERTICAL STRESS			No. of Data
	Average	SS	SD	Average	SS	SD	Average	SS	SD	
<b>Train</b>	0.1767	321.27	0.299	213.66	1017057500	531.52	-12.53	1323848	19.18	3600
<b>Test</b>	0.0092	22.50	0.114	239.17	309618240	423.29	-7.73	334846	13.92	1728
<b>Total</b>	0.1493	352.14	0.257	221.93	1327434400	499.14	-10.97	1685653	17.79	5328

$R/H_2$  : 0.2, 0.4, 0.8, 1.2, 1.8, 2.4

$H_1/H_2$  : 0.5, 1.0, 1.5, 2.0, 4.0, 5.0

$E_2/E_3$  ,  $E_1/E_2$  : 0.5, 1.0, 2.0, 5.0, 10, 30, 50, 90, 140, 170.

# DISPLACEMENT ( TRAINING )



### DISPLACEMENT

$\epsilon_{\max}$	CPU / 20 (Sec)	RMS (Train)	$R^2$ (Train)	$\bar{\sigma}$ (Train)	Subdomain	Parameters	RMS (Test)	$R^2$ (Test)	$\bar{\sigma}$ (Test)	$R^2$ (Total)
0.01	85	0.0015	1.000	0.002	1290	2935	0.063	0.695	0.093	0.980
0.10	15	0.0150	0.997	0.016	335	1220	0.058	0.742	0.084	0.981
0.15	12	0.0200	0.996	0.021	268	1012	0.055	0.768	0.078	0.982
0.30	9	0.0320	0.989	0.031	170	700	0.060	0.724	0.088	0.972

### A. 3-Layer System Data Generated from Multiple BISAR Runs

There are two files:

bsr.dat is the data to be used for data fitting.

bsr.tes is the data to be used for testing after the model is developed.

This is a 3 layer system with E1, E2, E3, h1, h2, and r (radius of loaded area) An standard load was considered. There are seven columns in each data set.

The first 4 columns are inputs as follows:

1 - K1: (E1/E2) from .5 to 170

2 - K2: (E2/E3) from .5 to 170

3 - H : (h1/h2) from .2 to 2.4

4 - A : ( r/h2) from .5 to 5

Columns 5 to 7 are outputs as follows

5 - D0: Deflection at the center of load

6 - H : Horizontal strain at the bottom of layer 1

7 - V : Vertical strain at the bottom of layer 1

### B. AASHO Road Test Data

There are three files:

pav.dat is the data to be used for data fitting. (7592 records, about 80%)

pav.tes is the data to be used for testing after the model is developed.  
(1872 records, about 20%)

pavall.dat contains all the data in the above files and also sorted by section number and indexday. This file can also be used for data fitting and then sensitivity analysis afterwards.

There are eleven columns in each data set.

The first 10 columns are inputs as follows:

1 - loopnum: loop number from 1 to 6

2 - lane: 1 for inner lane, 2 for outer lane

3 - thick: surface thickness in inches

4 - basethk: base thickness in inches

5 - subasthk: subbase thickness in inches

6 - sect: test section number

7 - indexday: indexday for the AASHO Road test from 1 to 55

8 - wtappl: total number of weighted application

9 - load: axle load in kips

10- l2t: 0 for no load, 1 for single-axle, 2 for tandem-axle

Column 11 is the response, PSI

"loess1.5"

Call:  
loess(formula = D0 ~ K1 \* K2 \* H \* A, span = 0.5, degree = 2, normalize = F)

Number of Observations: 3600  
Equivalent Number of Parameters: 42.7  
Residual Standard Error: 0.2055  
Multiple R-squared: 0.54  
Residuals:  
min 1st Q median 3rd Q max  
-0.4068 -0.02105 0.005336 0.03958 2.132

pav.loess

Call:  
loess(formula = D0 ~ K1 \* K2 \* H \* A, span = 0.1, degree = 2, normalize = F)

Number of Observations: 3600  
Equivalent Number of Parameters: 16.1  
Residual Standard Error: 0.07764  
Multiple R-squared: 0.96  
Residuals:  
min 1st Q median 3rd Q max  
-0.5723 -0.01265 -0.001217 0.01181 0.3155

pav.loess2

Call:  
loess(formula = D0 ~ K1 \* K2 \* H \* A, span = 0.05, degree = 2, normalize = F,  
trace.hat = "approximate")

Number of Observations: 3600  
Equivalent Number of Parameters: 14.9  
Residual Standard Error: 0.05245  
Multiple R-squared: 0.98  
Residuals:  
min 1st Q median 3rd Q max  
-0.5722 -0.01015 0.00004293 0.01118 0.2342

pav.loess3

Call: lm(formula = D0 ~ predict(pav.loess3))  
Residuals:

Min 1Q Median 3Q Max  
-0.4452 -0.01553 -0.006186 0.008473 0.3369

Coefficients:

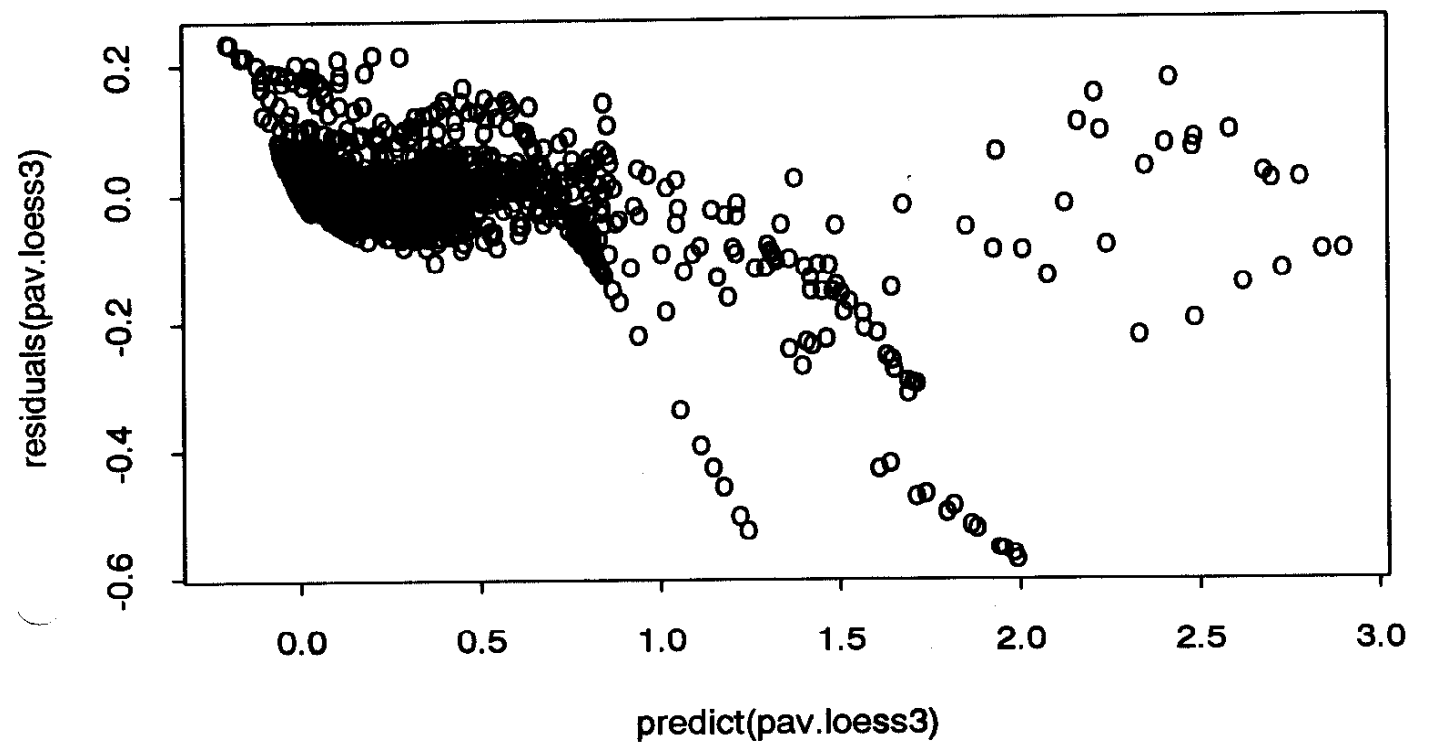
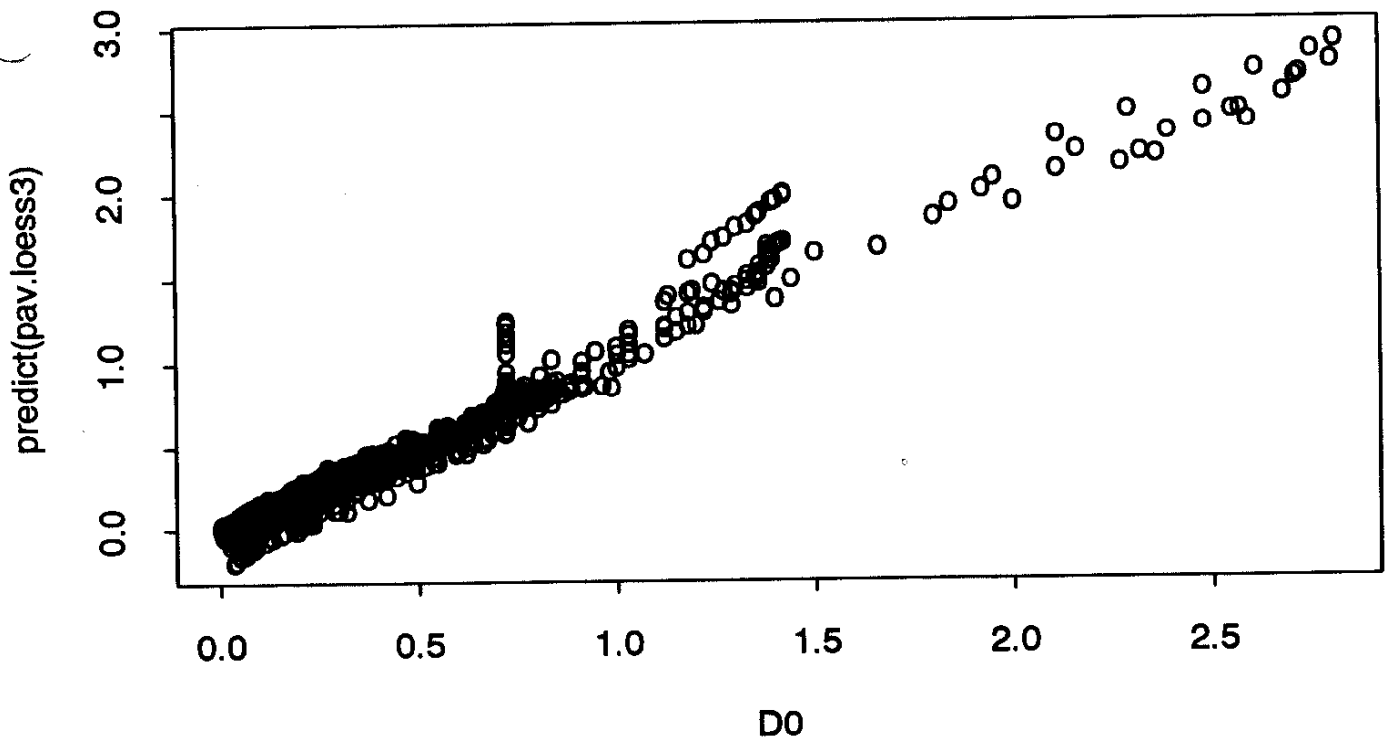
	Value	Std. Error	t value	Pr(> t )
(Intercept)	0.0121	0.0009	13.5345	0.0000
predict(pav.loess3)	0.9274	0.0025	376.7569	0.0000

Residual standard error: 0.04698 on 3598 degrees of freedom  
Multiple R-Squared: 0.9753

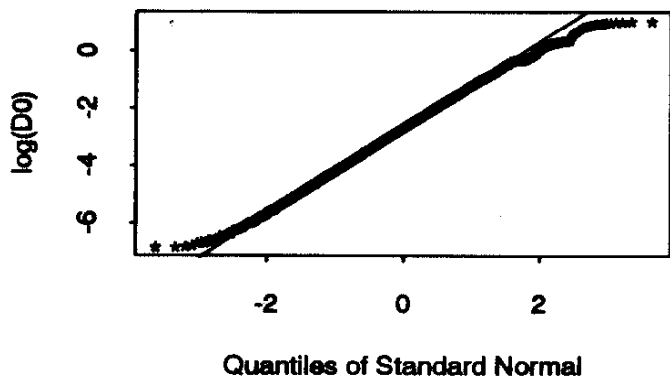
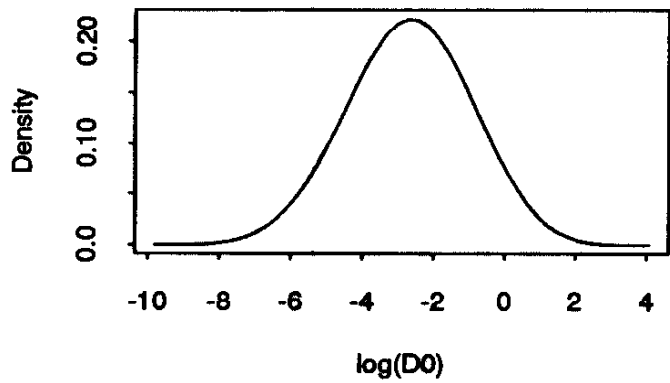
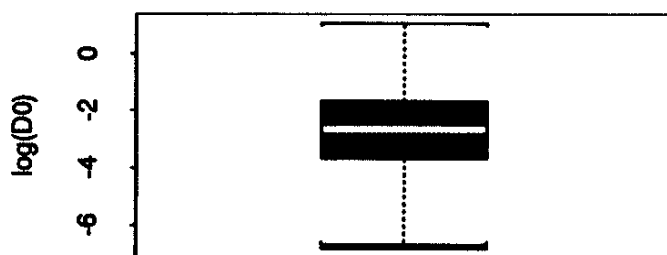
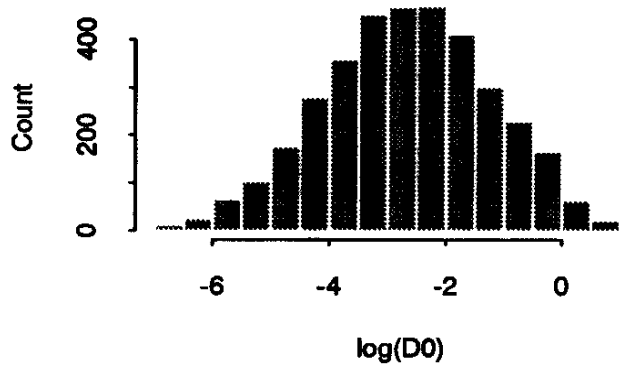
Correlation of Coefficients:  
(Intercept)  
predict(pav.loess3) -0.4872

LOESS Algorithm:

Prediction Based On Original DB (3600 pts)



For Reflectionism





```

source("loess4.s")
pav> #pav.loess <- loess(D0 ~ K1 * K2 * H * A, span=0.5, degree=2, normalize=F)
#pav.loess2 <- update(pav.loess, span=0.1)
#pav.loess3 <- update(pav.loess2, span=0.05, trace.hat="approximate")
#print(pav.loess)
#print(pav.loess2)
#print(pav.loess3)
#fit3 <- summary(lm(D0 ~ predict(pav.loess3)))
#print(fit3)
#pav.loess4 <- update(pav.loess3, formula=log(D0)-log(K1)*log(K2)*H*A)
pred <- predict(pav.loess4)
pav> pred.tes <- predict(pav.loess4, pav.tes)
pav> fit4 <- summary(lm(log(D0) ~ pred))
pav> fit4.tes <- summary(lm(log(D0T) ~ pred.tes))
pav> print(fit4)

```

Call: lm(formula = log(D0) ~ pred)

Residuals:

Min	1Q	Median	3Q	Max
-0.09384	-0.03058	0.002553	0.0214	0.1599

Coefficients:

	Value	Std. Error	t value	Pr(> t )
(Intercept)	-0.0139	0.0014	-9.7554	0.0000
pred	0.9962	0.0005	2116.1744	0.0000

Residual standard error: 0.04083 on 3598 degrees of freedom

Multiple R-Squared: 0.9992

Correlation of Coefficients:

(Intercept)

pred 0.8793

pav> print(fit4.tes)

Call: lm(formula = log(D0T) ~ pred.tes)

Residuals:

Min	1Q	Median	3Q	Max
-0.08679	-0.03371	-0.006159	0.02943	0.1823

Coefficients:

	Value	Std. Error	t value	Pr(> t )
(Intercept)	-0.0753	0.0029	-26.1181	0.0000
pred.tes	0.9845	0.0009	1088.4228	0.0000

Residual standard error: 0.04415 on 1726 degrees of freedom

Multiple R-Squared: 0.9985

Correlation of Coefficients:

(Intercept)

pred.tes 0.9296

pav> fit4.d0 <- summary(lm(D0 ~ exp(pred)))

pav> fit4.tes.d0 <- summary(lm(D0T ~ exp(pred.tes)))

pav> print(fit4.d0)

Call: lm(formula = D0 ~ exp(pred))

Residuals:

Min	1Q	Median	3Q	Max
-0.1426	-0.001368	0.0005445	0.00168	0.132

Coefficients:

	Value	Std. Error	t value	Pr(> t )
(Intercept)	-0.0006	0.0002	-4.0562	0.0001
exp(pred)	0.9979	0.0005	2215.7563	0.0000

Residual standard error: 0.008086 on 3598 degrees of freedom

Multiple R-Squared: 0.9993

Correlation of Coefficients:

```
(Intercept)
exp(pred) -0.5107
pav> print(fit4.tes.d0)
```

```
Call: lm(formula = DOT ~ exp(pred.tes))
```

```
Residuals:
    Min       1Q   Median       3Q      Max
-0.01978 -0.000998  0.000328  0.001669  0.03043
```

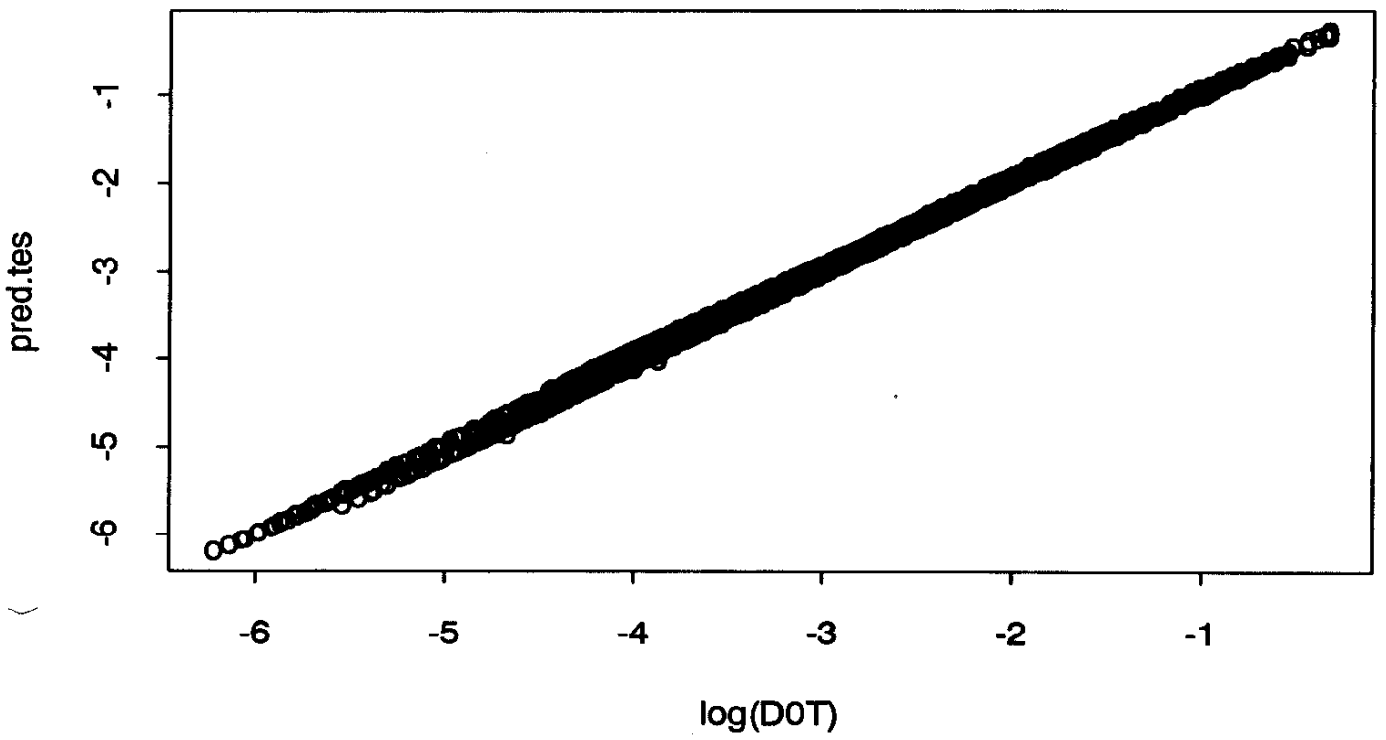
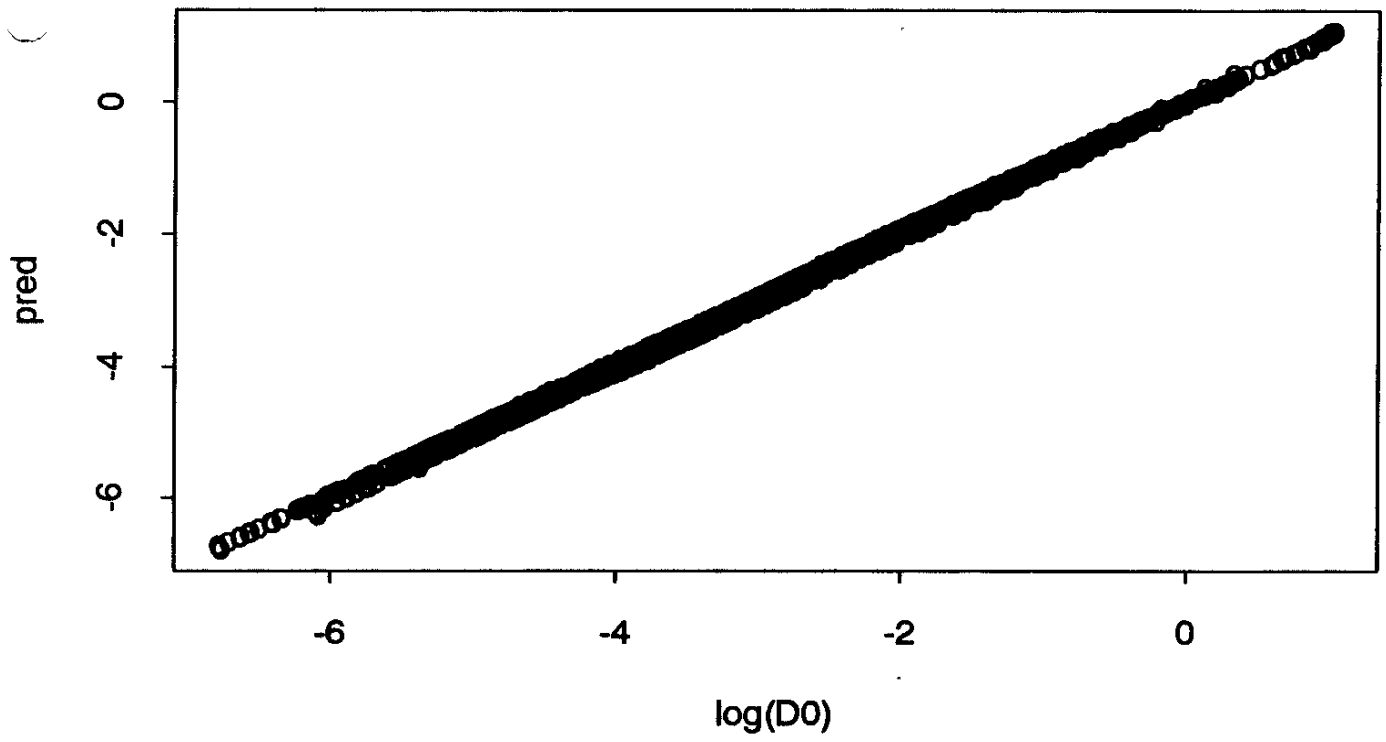
Coefficients:

	Value	Std. Error	t value	Pr(> t )
(Intercept)	-0.0006	0.0001	-5.4184	0.0000
exp(pred.tes)	0.9698	0.0008	1226.1851	0.0000

```
Residual standard error: 0.003866 on 1726 degrees of freedom
Multiple R-Squared: 0.9989
```

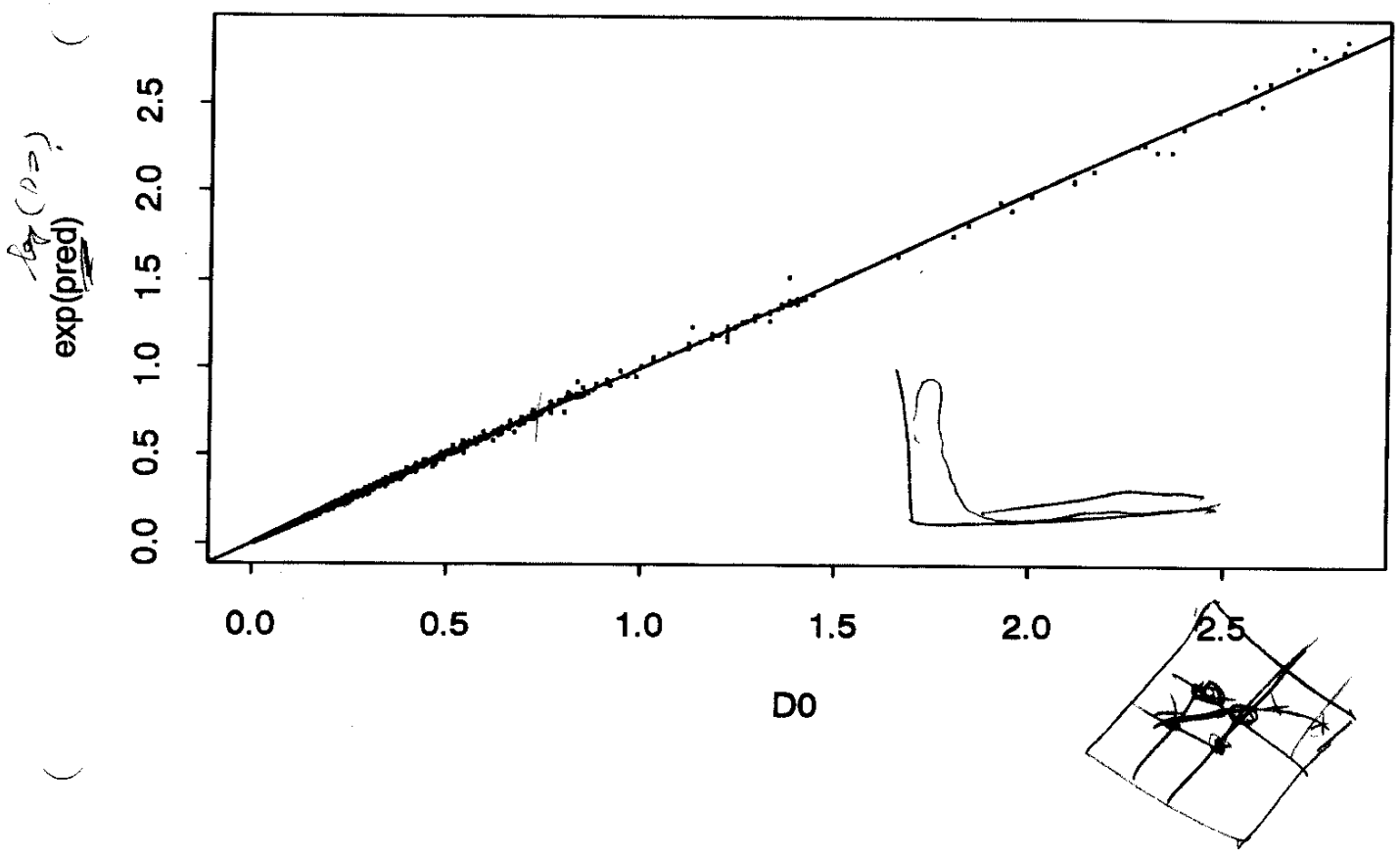
Correlation of Coefficients:

```
(Intercept)
exp(pred.tes) -0.6309
pav> postscript("loess4.ps1")
pav> oldpar <- par(mfrow = c(2, 1))
pav> plot(log(D0), pred)
pav> plot(log(DOT), pred.tes)
pav> par(oldpar)
pav> graphics.off()
pav> vga()
Set up for DOS graphics mode 12h, graphics buffer: 153600 bytes.
sink()
```



$N = 3600$ ,  $SEE = 0.008086$ ,  $R^2 = 0.9993$

Local Regression



$N = 1728$ ,  $SEE = 0.003866$ ,  $R^2 = 0.9999$

