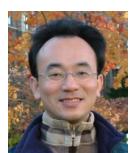


Big Data Mining 巨量資料探勘



關連分析 (Association Analysis)

1072DM05 MI4 (M2244) (2849) Wed 6, 7 (13:10-15:00) (B206)



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http://mail. tku.edu.tw/myday/ 2019/03/20

課程大綱 (Syllabus)

週次(Week) 日期(Date) 內容(Subject/Topics)

- 1 2019/02/20 巨量資料探勘課程介紹 (Course Orientation for Big Data Mining)
- 2 2019/02/27 AI人工智慧與大數據分析 (Artificial Intelligence and Big Data Analytics)
- 3 2019/03/06 分群分析 (Cluster Analysis)
- 4 2019/03/13 個案分析與實作一(SAS EM 分群分析): Case Study 1 (Cluster Analysis - K-Means using SAS EM)
- 5 2019/03/20 關連分析 (Association Analysis)
- 6 2019/03/27 個案分析與實作二 (SAS EM 關連分析): Case Study 2 (Association Analysis using SAS EM)
- 7 2019/04/03 教學行政觀摩日 (Off-campus study)
- 8 2019/04/10 分類與預測(Classification and Prediction)

課程大綱 (Syllabus)

週次(Week) 日期(Date) 內容(Subject/Topics)

- 9 2019/04/17 期中報告 (Midterm Project Presentation)
- 10 2019/04/24 期中考試週 (Midterm Exam)
- 11 2019/05/01 個案分析與實作三 (SAS EM 決策樹、模型評估): Case Study 3 (Decision Tree, Model Evaluation using SAS EM)
- 12 2019/05/08 個案分析與實作四 (SAS EM 迴歸分析、類神經網路): Case Study 4 (Regression Analysis, Artificial Neural Network using SAS EM)
- 13 2019/05/15 機器學習與深度學習
(Machine Learning and Deep Learning)
- 14 2019/05/22 期末報告 (Final Project Presentation)
- 15 2019/05/29 畢業考試週(Final Exam)

Transaction Database

Transaction ID	Items bought
T01	A, B, D
T02	A, C, D
T03	B, C, D, E
T04	A, B, D
T05	A, B, C, E
T06	A, C
T07	B, C, D
T08	B, D
T09	A, C, E
T10	B, D

Association Analysis

Data Mining Tasks & Methods

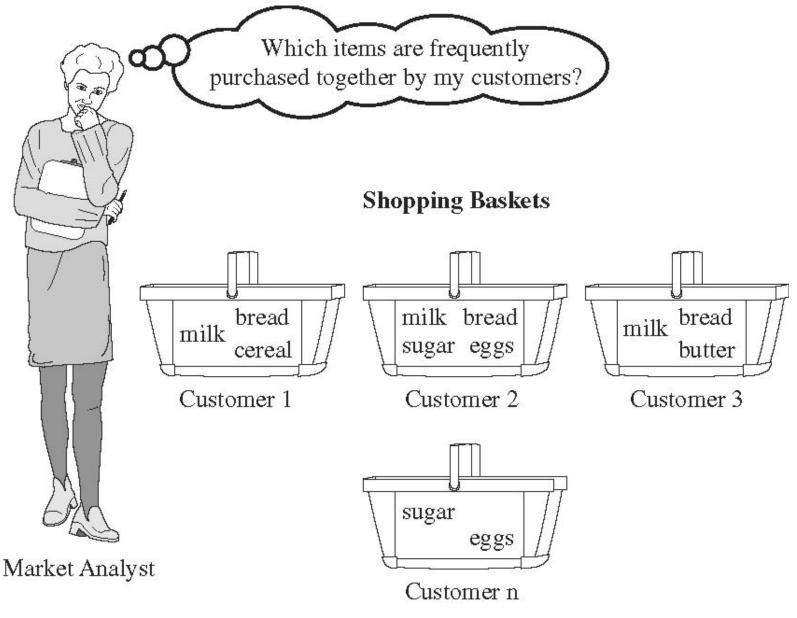
Data Mining Tasks & Methods	Data Mining Algorithms	Learning Type
Prediction		
Classification	Decision Trees, Neural Networks, Support Vector Machines, kNN, Naïve Bayes, GA	Supervised
Regression	Linear/Nonlinear Regression, ANN, Regression Trees, SVM, kNN, GA	Supervised
Time series	Autoregressive Methods, Averaging Methods, Exponential Smoothing, ARIMA	Supervised
Association		
Market-basket	Apriori, OneR, ZeroR, Eclat, GA	Unsupervised
Link analysis	Expectation Maximization, Apriori Algorithm, Graph-Based Matching	Unsupervised
Sequence analysis	Apriori Algorithm, FP-Growth, Graph-Based Matching	Unsupervised
Segmentation		
	k-means, Expectation Maximization (EM)	Unsupervised
Outlier analysis	k-means, Expectation Maximization (EM)	Unsupervised

Source: Ramesh Sharda, Dursun Delen, and Efraim Turban (2017), Business Intelligence, Analytics, and Data Science: A Managerial Perspective, 4th Edition, Pearson

Association Analysis: Mining Frequent Patterns, Association and Correlations

- Association Analysis
- Mining Frequent Patterns
- Association and Correlations
- Apriori Algorithm

Market Basket Analysis



• Apriori Algorithm

Raw Transact	Transaction Data		One-item Itemsets		Two-item I	temsets	Three-item	Itemsets
Transaction No	SKUs (Item No)		ltemset (SKUs)	Support	ltemset (SKUs)	Support	ltemset (SKUs)	Support
1	1, 2, 3, 4		1	3	1, 2	3	1, 2, 4	3
1	2, 3, 4		2	6	1, 3	2	2, 3, 4	3
1	2, 3		3	4	1, 4	3		
1	1, 2, 4		4	5	2, 3	4		
1	1, 2, 3, 4			-	2, 4	5		
1	2, 4				3, 4	3		

- A very popular DM method in business
- Finds interesting relationships (affinities) between variables (items or events)
- Part of machine learning family
- Employs unsupervised learning
- There is no output variable
- Also known as market basket analysis
- Often used as an example to describe DM to ordinary people, such as the famous "relationship between diapers and beers!"

- Input: the simple point-of-sale transaction data
- Output: Most frequent affinities among items
- Example: according to the transaction data...

"Customer who bought a laptop computer and a virus protection software, also bought extended service plan 70 percent of the time."

- How do you use such a pattern/knowledge?
 - Put the items next to each other for ease of finding
 - Promote the items as a package (do not put one on sale if the other(s) are on sale)
 - Place items far apart from each other so that the customer has to walk the aisles to search for it, and by doing so potentially seeing and buying other items

- A representative applications of association rule mining include
 - In business: cross-marketing, cross-selling, store design, catalog design, e-commerce site design, optimization of online advertising, product pricing, and sales/promotion configuration
 - In medicine: relationships between symptoms and illnesses; diagnosis and patient characteristics and treatments (to be used in medical DSS); and genes and their functions (to be used in genomics projects)...

• Are all association rules interesting and useful?

A Generic Rule: $X \Rightarrow Y [S\%, C\%]$

- **X, Y**: products and/or services
- **X:** Left-hand-side (LHS)
- Y: Right-hand-side (RHS)
- **S:** Support: how often **X** and **Y** go together
- **C:** Confidence: how often **Y** go together with the **X**

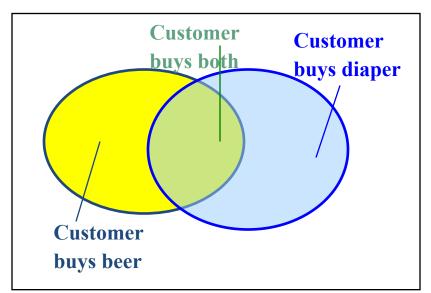
Example: {Laptop Computer, Antivirus Software} ⇒ {Extended Service Plan} [30%, 70%]

- Algorithms are available for generating association rules
 - Apriori
 - Eclat
 - FP-Growth
 - + Derivatives and hybrids of the three
- The algorithms help identify the frequent item sets, which are, then converted to association rules

- Apriori Algorithm
 - Finds subsets that are common to at least a minimum number of the itemsets
 - uses a bottom-up approach
 - frequent subsets are extended one item at a time (the size of frequent subsets increases from one-item subsets to two-item subsets, then three-item subsets, and so on), and
 - groups of candidates at each level are tested against the data for minimum

Basic Concepts: Frequent Patterns and Association Rules

Transaction-id	Items bought	
10	A, B, D	
20	A, C, D	
30	A, D, E	
40	B, E, F	
50	B, C, D, E, F	



- Itemset X = $\{x_1, ..., x_k\}$
- Find all the rules $X \rightarrow Y$ with minimum support and confidence
 - support, s, probability that a transaction contains $X \cup Y$
 - confidence, c, conditional probability that a transaction having X also contains Y

Let $sup_{min} = 50\%$, $conf_{min} = 50\%$ Freq. Pat.: {A:3, B:3, D:4, E:3, AD:3} Association rules:

> $A \rightarrow D$ (60%, 100%) $D \rightarrow A$ (60%, 75%)

 $A \rightarrow D$ (support = 3/5 = 60%, confidence = 3/3 = 100%) $D \rightarrow A$ (support = 3/5 = 60%, confidence = 3/4 = 75%)

Market basket analysis

- Example
 - Which groups or sets of items are customers likely to purchase on a given trip to the store?
- Association Rule
 - Computer → antivirus_software [support = 2%; confidence = 60%]
 - A support of 2% means that 2% of all the transactions under analysis show that computer and antivirus software are purchased together.
 - A confidence of 60% means that 60% of the customers who purchased a computer also bought the software.

Association rules

- Association rules are considered interesting if they satisfy both
 - a minimum support threshold and
 - a minimum confidence threshold.

Frequent Itemsets, Closed Itemsets, and Association Rules

Let $I = \{I_1, I_2, ..., I_m\}$ be a set of items. Let D, the task-relevant data, be a set of database transactions where each transaction T is a set of items such that $T \subseteq I$. Each transaction is associated with an identifier, called TID. Let A be a set of items. A transaction T is said to contain A if and only if $A \subseteq T$. An association rule is an implication of the form $A \Rightarrow B$, where $A \subset I, B \subset I$, and $A \cap B = \phi$. The rule $A \Rightarrow B$ holds in the transaction set D with support s, where s is the percentage of transactions in D that contain $A \cup B$ (i.e., the *union* of sets A and B, or say, both A and B). This is taken to be the probability, $P(A \cup B)$.¹ The rule $A \Rightarrow B$ has confidence c in the transaction set D, where c is the percentage of transaction set D, where c is the percentage of transaction set D, where c is the percentage of transaction set D, where c is the percentage of transaction set D, where c is the percentage of transaction set D, and $A \cup B$. The rule $A \Rightarrow B$ has confidence c in the transaction set D, where c is the percentage of transaction set D, where c is the percentage of transactions in D containing A that also contain B. This is taken to be the conditional probability, P(B|A). That is,

Support (A
$$\rightarrow$$
 B) = P(A \cup B)
Confidence (A \rightarrow B) = P(B|A)

Support $(A \rightarrow B) = P(A \cup B)$ Confidence $(A \rightarrow B) = P(B|A)$

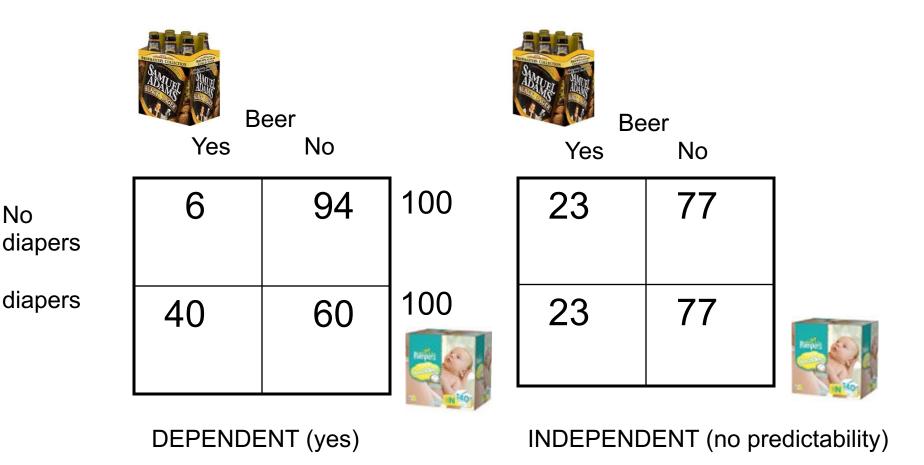
 The notation P(A ∪ B) indicates the probability that a transaction contains the union of set A and set B

- (i.e., it contains every item in A and in B).

• This should not be confused with P(A or B), which indicates the probability that a transaction contains either A or B.

Does diaper purchase predict beer purchase?

Contingency tables



Source: Dickey (2012) http://www4.stat.ncsu.edu/~dickey/SAScode/Encore_2012.ppt

Support $(A \rightarrow B) = P(A \cup B)$

Confidence $(A \rightarrow B) = P(B|A)$ Conf $(A \rightarrow B) = Supp (A \cup B) / Supp (A)$

Lift $(A \rightarrow B) = Supp (A \cup B) / (Supp (A) x Supp (B))$ Lift (Correlation) Lift $(A \rightarrow B) = Confidence (A \rightarrow B) / Support(B)$

Source: Dickey (2012) http://www4.stat.ncsu.edu/~dickey/SAScode/Encore_2012.ppt

Lift

Lift = Confidence / Expected Confidence if Independent

Checking	No (1500)	Yes (8500)	(10000)
No	500	3500	4000
Yes	1000	5000	6000

SVG=>CHKG Expect 8500/10000 = 85% if independent Observed Confidence is 5000/6000 = 83%Lift = 83/85 < 1.

Savings account holders actually LESS likely than others to have checking account !!!

Minimum Support and Minimum Confidence

- Rules that satisfy both a minimum support threshold (*min_sup*) and a minimum confidence threshold (*min_conf*) are called strong.
- By convention, we write support and confidence values so as to occur between 0% and 100%, rather than 0 to 1.0.

K-itemset

- itemset
 - A set of items is referred to as an itemset.
- K-itemset
 - An itemset that contains k items is a k-itemset.
- Example:
 - The set {computer, antivirus software} is a 2-itemset.

Absolute Support and Relative Support

- Absolute Support
 - The occurrence frequency of an itemset is the number of transactions that contain the itemset
 - frequency, support count, or count of the itemset
 - Ex: 3
- Relative support
 - Ex: 60%

Frequent Itemset

 If the relative support of an itemset *I satisfies* a prespecified minimum support threshold, then I is a frequent itemset.

– i.e., the absolute support of I satisfies the corresponding minimum support count threshold

 The set of frequent k-itemsets is commonly denoted by L_K

Confidence

 $confidence(A \Rightarrow B) = P(B|A) = \frac{support(A \cup B)}{support(A)} = \frac{support_count(A \cup B)}{support_count(A)}$

- the confidence of rule $A \rightarrow B$ can be easily derived from the support counts of A and $A \cup B$.
- once the support counts of A, B, and A ∪ B are found, it is straightforward to derive the corresponding association rules A →B and B →A and check whether they are strong.
- Thus the problem of mining association rules can be reduced to that of mining frequent itemsets.

Association rule mining: Two-step process

- 1. Find all frequent itemsets
 - By definition, each of these itemsets will occur at least as frequently as a predetermined minimum support count, *min_sup*.
- 2. Generate strong association rules from the frequent itemsets
 - By definition, these rules must satisfy minimum support and minimum confidence.

Efficient and Scalable Frequent Itemset Mining Methods

- The Apriori Algorithm
 - Finding Frequent Itemsets Using Candidate Generation

Apriori Algorithm

- Apriori is a seminal algorithm proposed by R. Agrawal and R. Srikant in 1994 for mining frequent itemsets for Boolean association rules.
- The name of the algorithm is based on the fact that the algorithm uses prior knowledge of frequent itemset properties, as we shall see following.

Apriori Algorithm

- Apriori employs an iterative approach known as a *level-wise search, where k-itemsets are used to explore (k+1)-itemsets.*
- First, the set of frequent 1-itemsets is found by scanning the database to accumulate the count for each item, and collecting those items that satisfy minimum support. The resulting set is denoted L₁.
- Next, L₁ is used to find L₂, the set of frequent 2-itemsets, which is used to find L₃, and so on, until no more frequent kitemsets can be found.
- The finding of each L_k requires one full scan of the database.

Apriori Algorithm

- To improve the efficiency of the level-wise generation of frequent itemsets, an important property called the Apriori property.
- Apriori property
 - All nonempty subsets of a frequent itemset must also be frequent.

Apriori algorithm (1) Frequent Itemsets (2) Association Rules

Transaction Database

Transaction ID	Items bought
T01	A, B, D
T02	A, C, D
T03	B, C, D, E
T04	A, B, D
T05	A, B, C, E
T06	A, C
T07	B, C, D
T08	B, D
T09	A, C, E
T10	B, D

Table 1 shows a database with 10 transactions.

Let *minimum support* = 20% and *minimum confidence* = 80%. Please use **Apriori algorithm** for generating **association rules** from frequent itemsets.

Table 1: Transaction Database

Transaction	Items bought
ID	
T01	A, B, D
T02	A, C, D
T03	B, C, D, E
Т04	A, B, D
T05	A, B, C, E
Т06	A, C
T07	B, C, D
T08	B, D
T09	Α, Ϲ, Ε
T10	B, D

Transaction ID	Items bought
T01	A, B, D
Т02	A, C, D
Т03	B, C, D, E
Т04	A, B, D
Т05	A, B, C, E
Т06	Α, C
Т07	B, C, D
Т08	B, D
Т09	Α, Ϲ, Ε
T10	B, D

Е

3

Apriori Algorithm $C_1 \rightarrow L_1$



C ₁			L ₁	
ltemset	Support Count	minimum support = 20%	ltemset	Support Count
А	6	= 2 / 10 Min. Support	A	6
В	7	Count = 2	В	7
С	6	\longrightarrow	С	6
D	7		D	7

Ε

3

Transaction	Items
ID	bought
T01	A, B, D
Т02	A, C, D
Т03	B, C, D, E
Т04	A, B, D
Т05	A, B, C, E
т06	Α, C
Т07	B, C, D
Т08	B, D
т09	A, C, E
Т10	B, D

Itemset	Support Count
А	6
В	7
C	6
D	7
E	3

 C_2

Itemset	Support Count
А, В	3
A, C	4
A, D	3
Α, Ε	2
В, С	3
B, D	6
В, Е	2
C, D	3
С, Е	3
D, E	1

minimum support = 20% = 2 / 10 Min. Support Count = 2

ltemset	Support Count
А, В	3
A, C	4
A, D	3
Α, Ε	2
В, С	3
B, D	6
В, Е	2
C, D	3
С, Е	3

 L_2

Transaction	Items
Transaction	items
ID	bought
Т01	A, B, D
т02	A, C, D
Т03	B, C, D, E
т04	A, B, D
Т05	A, B, C, E
т06	А, С
Т07	B, C, D
т08	B, D
т09	A, C, E
T10	B, D

-2

Itemset	Support Count
А, В	3
A, C	4
A, D	3
Α, Ε	2
В, С	3
B, D	6
В, Е	2
C, D	3
С, Е	3

Apriori Algorithm $C_3 \rightarrow L_3$



 C_3

Itemset	Support Count
А, В, С	1
A, B, D	2
A, B, E	1
A, C, D	1
A, C, E	2
B, C, D	2
В, С, Е	2

minimum support = 20%= 2 / 10 Min. Support Count = 2

Count A, B, D A, C, E B, C, D В, С, Е

 L_3

Itemset

Support

2

2

2

2

Transaction	Items
ID	bought
T01	A, B, D
т02	A, C, D
Т03	B, C, D, E
Т04	A, B, D
Т05	A, B, C, E
т06	A, C
Т07	B, C, D
Т08	B, D
т09	A, C, E
Т10	B, D

Generating Association Rules

minimum confidence = 80%

		L ₂				
L_1		Itemset	Support Count			
Itemset	Support	А, В	3			
A	Count 6	A, C	4			
В	7	A, D	3			
С	6	Α, Ε	2			
D	7	B, C	3			
E	3	B, D	6			
		B, E	2			
		C, D	3			

С, Е

3

Association Rules Generated from L_2

	
A→B: 3/6	B→A: 3/7
A→C: 4/6	C→A: 4/6
A→D: 3/6	D→A: 3/7
A→E: 2/6	E→A: 2/3
B→C: 3/7	C→B: 3/6
B→D: 6/7=85.7% *	D→B: 6/7=85.7% *
B→E: 2/7	E→B: 2/3
C→D: 3/6	D→C: 2/7
C→E: 3/6	E→C: 3/3=100% *

Step **2-1**

Transaction	Items
ID	bought
T01	A, B, D
Т02	A, C, D
Т03	B, C, D, E
Т04	A, B, D
Т05	A, B, C, E
т06	Α, C
Т07	B, C, D
Т08	B, D
т09	A, C, E
T10	B, D

Generating Association Rules

minimum confidence = 80%

Association Rules Generated from L_3

		A→BD: 2/6	B→CD: 2/7
		B→AD: 2/7	C→BD: 2/6
		D→AB: 2/7	D→BC: 2/7
		AB→D: 2/3	BC→D: 2/3
t		AD→B: 2/3	BD→C: 2/6
		BD→A: 2/6	CD→B: 2/3
		A→CE: 2/6	B→CE: 2/7
		C→AE: 2/6	C→BE: 2/6
	7	E→AC: 2/3	E→BC: 2/3
		AC→E: 2/4	BC→E: 2/3
		AE→C: 2/2=100%*	BE→C: 2/2=100%*
		CE→A: 2/3	CE→B: 2/3

L_1		L_2		L
ltemset	Support Count	Itemset	Support Count	lter
А	6	А, В	3	
В	7	А, С	4	Α,
С	6	A, D	3	Α,
D	7	Α, Ε	2	В, (
Е	3	В, С	3	
		B, D	6	Β,
		В, Е	2	
		C, D	3	
		С, Е	3	

L ₃	
Itemset	Support Count
A, B, D	2
A, C, E	2
B, C, D	2
В, С, Е	2

Step **2-2**

Transaction ID T01	Items bought A, B, D	Frequent I	tem	sets		and	Ass	ociatio	on Rule
T02	A, C, D								
Т03	B, C, D, E		-1			-2		-3	
Т04	A, B, D		-		ſ				
Т05	А, В, С, Е		Itemset	Support		Itemset	Support	Itemset	Support
т06	A, C			Count			Count		Count
Т07	B, C, D		A	6		А, В	3		Count
Т08	B, D		В	7		A, C	4		2
Т09	A, C, E			,		,,,,		A, B, D	2
T10	B, D		C	6		A, D	3		
			D	7		Α, Ε	2	A, C, E	2
			E	3		В, С	3	B, C, D	2

B, D

В, Е С, D

C, E

6

2

3

3

B, C, E

2

minimum support = 20% minimum confidence = 80%

Association Rules:

B→D (60%, 85.7%) (Sup.: 6/10, Conf.: 6/7) D→B (60%, 85.7%) (Sup.: 6/10, Conf.: 6/7) E→C (30%, 100%) (Sup.: 3/10, Conf.: 3/3) AE→C (20%, 100%) (Sup.: 2/10, Conf.: 2/2) BE→C (20%, 100%) (Sup.: 2/10, Conf.: 2/2) Table 1 shows a database with 10 transactions.

Let *minimum support* = 20% and *minimum confidence* = 80%.

Please use **Apriori algorithm** for generating **association rules** from frequent itemsets.

Transaction ID	Items bought
T01	A, B, D
T02	A, C, D
Т03	B, C, D, E
T04	A, B, D
T05	A, B, C, E
Т06	A, C
T07	B, C, D
T08	B, D
Т09	A, C, E
T10	B, D

Association Rules:

B→D (60%, 85.7%) (Sup.: 6/10, Conf.: 6/7) D→B (60%, 85.7%) (Sup.: 6/10, Conf.: 6/7) E→C (30%, 100%) (Sup.: 3/10, Conf.: 3/3) AE→C (20%, 100%) (Sup.: 2/10, Conf.: 2/2) BE→C (20%, 100%) (Sup.: 2/10, Conf.: 2/2)

Summary

- Association Analysis
- Apriori algorithm
 - -Frequent Itemsets
 - **–Association Rules**

References

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