Chapter Fifteen

Market Demand

From Individual to Market Demand Functions

- Think of an economy containing n consumers, denoted by i = 1, ... ,n.
- Consumer i's ordinary demand function for commodity j is

 $\boldsymbol{x}_{j}^{*i}(\boldsymbol{p}_{1},\boldsymbol{p}_{2},\boldsymbol{m}^{i})$

From Individual to Market Demand Functions

 Demand Functions
 When all consumers are price-takers, the market demand function for commodity j is

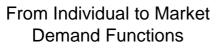
$$X_{j}(p_{1},p_{2},m^{1},\Lambda,m^{n}) = \sum_{i=1}^{n} x_{j}^{*i}(p_{1},p_{2},m^{i}).$$

• Aggregate demand depend on prices and the distribution of incomes

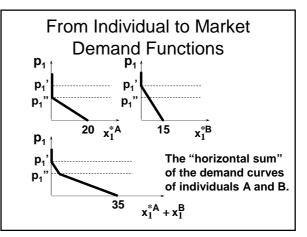
From Individual to Market

 Demand Functions
 If all consumers are identical then where M = nm or a constant proportion of individual income.

$$X_{j}(p_{1},p_{2},M) = n \times x_{j}^{*}(p_{1},p_{2},m)$$



- The market demand curve is the "horizontal sum" of the individual consumers' demand curves.
- E.g. suppose there are only two consumers; i = A,B.



Elasticities

- Elasticity measures the "sensitivity" of one variable with respect to another.
- The elasticity of variable X with respect to variable Y is

$$\varepsilon_{\mathbf{x},\mathbf{y}} = \frac{\%\Delta\mathbf{x}}{\%\Delta\mathbf{y}}.$$

Economic Applications of

- Elasticity
 Economists use elasticities to measure the sensitivity of
 - quantity demanded of commodity i with respect to the price of commodity i (ownprice elasticity of demand)
 - demand for commodity i with respect to the price of commodity j (cross-price elasticity of demand).

Economic Applications of Elasticity

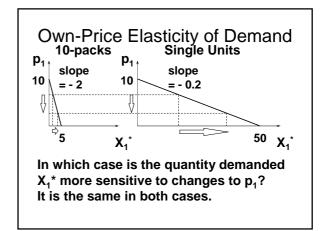
- demand for commodity i with respect to income (income elasticity of demand)
- quantity supplied of commodity i with respect to the price of commodity i (own-price elasticity of supply)

Economic Applications of Elasticity

- quantity supplied of commodity i with respect to the wage rate (elasticity of supply with respect to the price of labor)
- and many, many others.

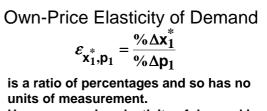
Own-Price Elasticity of Demand

• Q: Why not use a demand curve's slope to measure the sensitivity of quantity demanded to a change in a commodity's own price?



Own-Price Elasticity of Demand

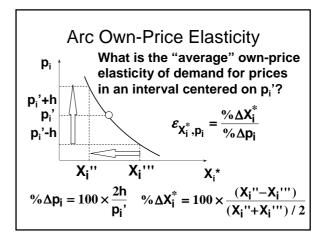
- Q: Why not just use the slope of a demand curve to measure the sensitivity of quantity demanded to a change in a commodity's own price?
- A: Because the value of sensitivity then depends upon the (arbitrary) units of measurement used for quantity demanded.

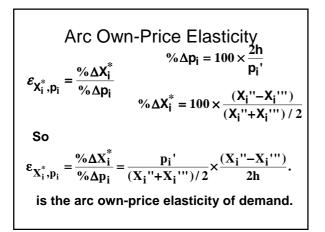


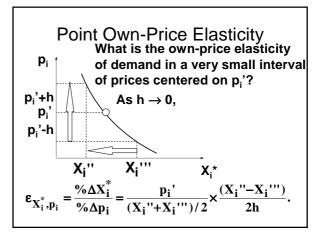
Hence own-price elasticity of demand is a sensitivity measure that is independent of units of measurement.

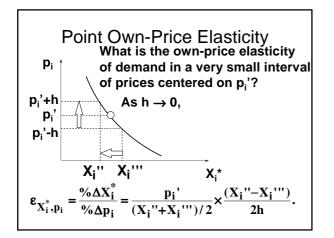
Arc and Point Elasticities

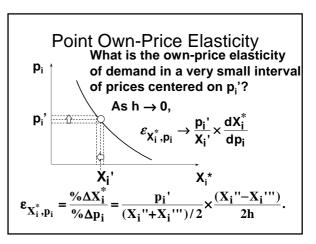
- An "average" own-price elasticity of demand for commodity i over an interval of values for p_i is an arc-elasticity, usually computed by a mid-point formula.
- Elasticity computed for a single value of p_i is a point elasticity.

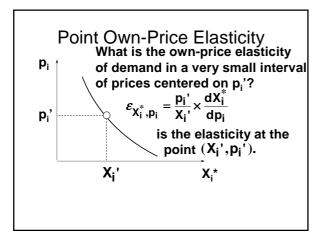








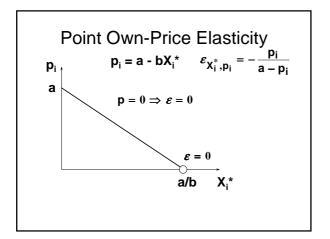


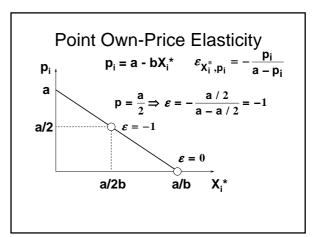


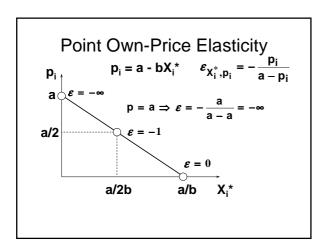
Point Own-Price Elasticity

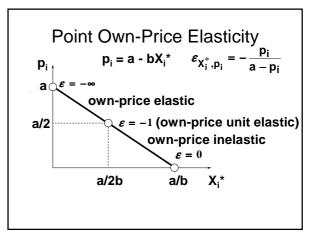
$$\varepsilon_{\chi_{i}^{*},p_{i}} = \frac{p_{i}}{\chi_{i}^{*}} \times \frac{dX_{i}}{dp_{i}}$$

E.g. Suppose $p_{i} = a - bX_{i}$.
Then $X_{i} = (a-p_{i})/b$ and
 $\frac{dX_{i}^{*}}{dp_{i}} = -\frac{1}{b}$. Therefore,
 $\varepsilon_{\chi_{i}^{*},p_{i}} = \frac{p_{i}}{(a-p_{i})/b} \times \left(-\frac{1}{b}\right) = -\frac{p_{i}}{a-p_{i}}$.

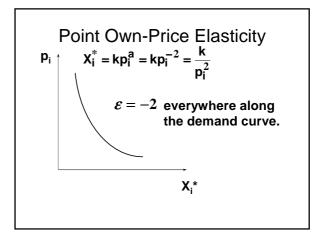








Point Own-Price Elasticity $\varepsilon_{\chi_i^*,p_i} = \frac{p_i}{\chi_i^*} \times \frac{dX_i}{dp_i}$ E.g. $X_i^* = kp_i^a$. Then $\frac{dX_i^*}{dp_i} = ap_i^{a-1}$ so $\varepsilon_{\chi_i^*,p_i} = \frac{p_i}{kp_i^a} \times kap_i^{a-1} = a\frac{p_i^a}{p_i^a} = a$.



Revenue and Own-Price Elasticity of Demand

- If raising a commodity's price causes little decrease in quantity demanded, then sellers' revenues rise.
- Hence own-price inelastic demand causes sellers' revenues to rise as price rises.

Revenue and Own-Price Elasticity of Demand

- If raising a commodity's price causes a large decrease in quantity demanded, then sellers' revenues fall.
- Hence own-price elastic demand causes sellers' revenues to fall as price rises.

Revenue and Own-Price Elasticity of Demand Sellers' revenue is $R(p) = p \times X^*(p)$. So $\frac{dR}{dp} = X^*(p) + p \frac{dX^*}{dp}$ $= X^*(p) \left[1 + \frac{p}{X^*(p)} \frac{dX^*}{dp} \right]$ $= X^*(p) [1 + \varepsilon].$

Revenue and Own-Price
Elasticity of Demand
$$\frac{dR}{dp} = X^*(p)[1 + \varepsilon]$$

so if $\varepsilon = -1$ then $\frac{dR}{dp} = 0$
and a change to price does not alter
sellers' revenue.

Revenue and Own-Price Elasticity of Demand $\frac{dR}{dp} = X^*(p)[1 + \varepsilon]$ but if $-1 < \varepsilon \le 0$ then $\frac{dR}{dp} > 0$ and a price increase raises sellers' revenue. Revenue and Own-Price Elasticity of Demand $\frac{dR}{dp} = X^*(p)[1 + \varepsilon]$ And if $\varepsilon < -1$ then $\frac{dR}{dp} < 0$ and a price increase reduces sellers' revenue.

Revenue and Own-Price Elasticity of Demand In summary:

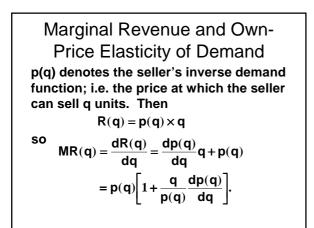
Own-price inelastic demand; $-1 < \varepsilon \le 0$ price rise causes rise in sellers' revenue. Own-price unit elastic demand; $\varepsilon = -1$ price rise causes no change in sellers' revenue.

Own-price elastic demand; $\varepsilon < -1$ price rise causes fall in sellers' revenue.

Marginal Revenue and Own-Price Elasticity of Demand

• A seller's marginal revenue is the rate at which revenue changes with the number of units sold by the seller.

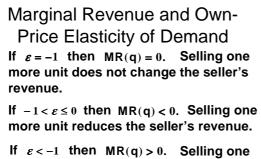
$$\mathsf{MR}(\mathsf{q}) = \frac{\mathsf{dR}(\mathsf{q})}{\mathsf{dq}}.$$



Marginal Revenue and Own-
Price Elasticity of Demand
$$MR(q) = p(q) \left[1 + \frac{q}{p(q)} \frac{dp(q)}{dq} \right].$$
and $\varepsilon = \frac{dq}{dp} \times \frac{p}{q}$ so $MR(q) = p(q) \left[1 + \frac{1}{\varepsilon} \right].$

Marginal Revenue and Own-Price Elasticity of Demand $MR(q) = p(q) \left[1 + \frac{1}{\epsilon} \right]$ says that the rate at which a seller's revenue changes with the number of units it sells depends on the sensitivity of quantity demanded to price; *i.e.*, upon the of the own-price elasticity of demand.

Marginal Revenue and Own-Price Elasticity of Demand $MR(q) = p(q) \left[1 + \frac{1}{\epsilon} \right]$ If $\epsilon = -1$ then MR(q) = 0. If $-1 < \epsilon \le 0$ then MR(q) < 0. If $\epsilon < -1$ then MR(q) > 0.



more unit raises the seller's revenue.

Marginal Revenue and Own-Price Elasticity of Demand An example with linear inverse demand. p(q) = a - bq. Then R(q) = p(q)q = (a - bq)q

and MR(q) = a - 2bq.

